

Lecture 8

Intro. to Combinational Blocks

Revised by WJ Han

Combinational Logic Design Practices

- **We will learn some basic combinational logic blocks and study how to design them.**
 - **Decoder**
 - **Encoder**
 - **Multiplexer**
 - **Demultiplexer**
 - **Adders/Subtractors**
 - **Multipliers**

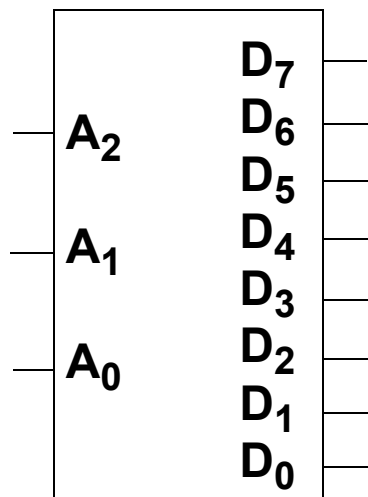
Design Procedure

- 1) Determine the specification.**
- 2) Determine the required inputs and outputs.**
- 3) Derive the truth table.**
- 4) Obtain the simplified Boolean functions.**
Use K-Map or inspection in this step.
- 5) Draw the logic diagram.**

A Decoder

- **A decoder** : a combinational circuit that converts n coded binary inputs to m ($m \leq 2^n$) unique outputs. We call it n -to- m decoder.

Example. 3-to-8 Decoder



Inputs			Outputs							
A_2	A_1	A_0	D_7	D_6	D_5	D_4	D_3	D_2	D_1	D_0
0	0	0	0	0	0	0	0	0	0	1
0	0	1	0	0	0	0	0	0	1	0
0	1	0	0	0	0	0	0	1	0	0
0	1	1	0	0	0	0	1	0	0	0
1	0	0	0	0	0	1	0	0	0	0
1	0	1	0	0	1	0	0	0	0	0
1	1	0	0	1	0	0	0	0	0	0
1	1	1	1	0	0	0	0	0	0	0

3-to-8 Decoder Implementation

We have to make K-Map for each D outputs. But this case is too simple.

$$D_0 = \bar{A}_2 \bar{A}_1 \bar{A}_0$$

$$D_1 = \bar{A}_2 \bar{A}_1 A_0$$

$$D_2 = \bar{A}_2 A_1 \bar{A}_0$$

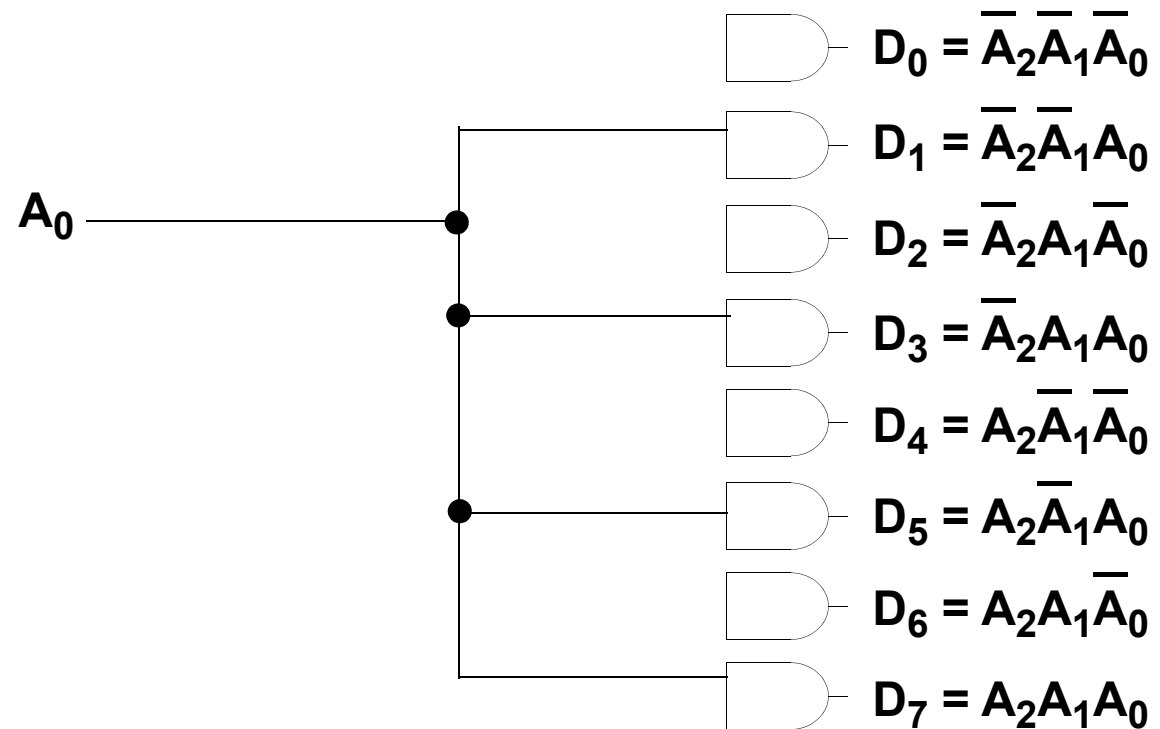
$$D_3 = \bar{A}_2 A_1 A_0$$

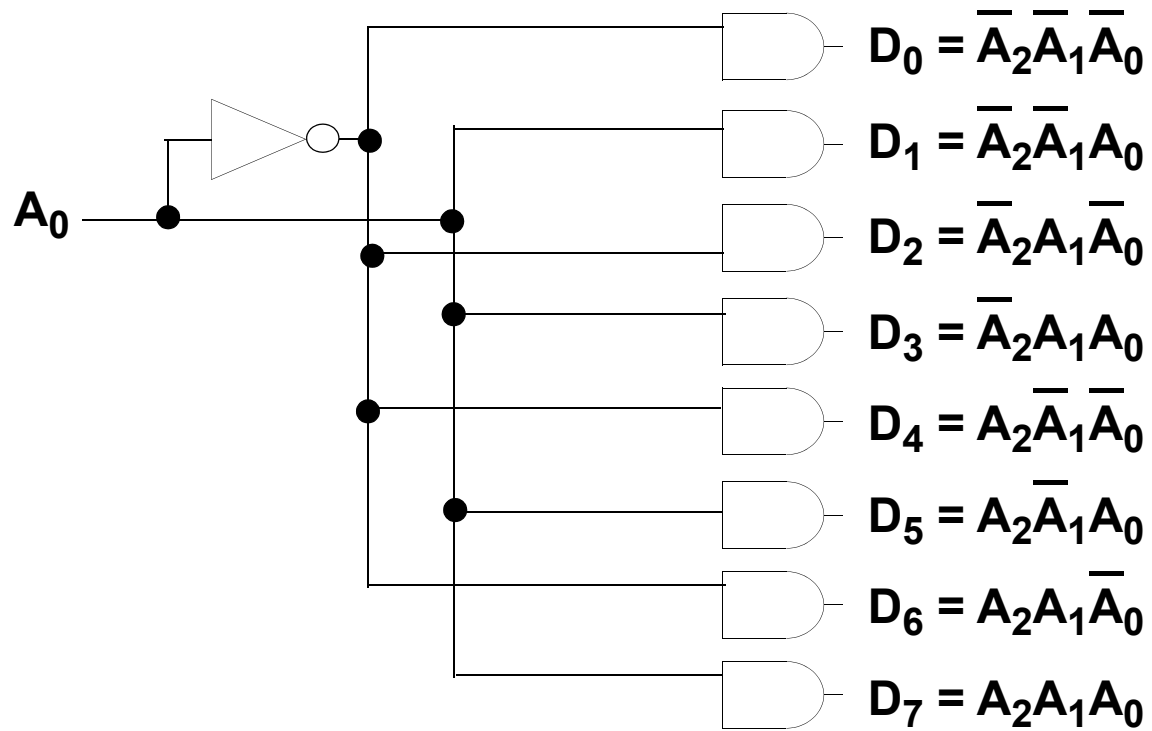
$$D_4 = A_2 \bar{A}_1 \bar{A}_0$$

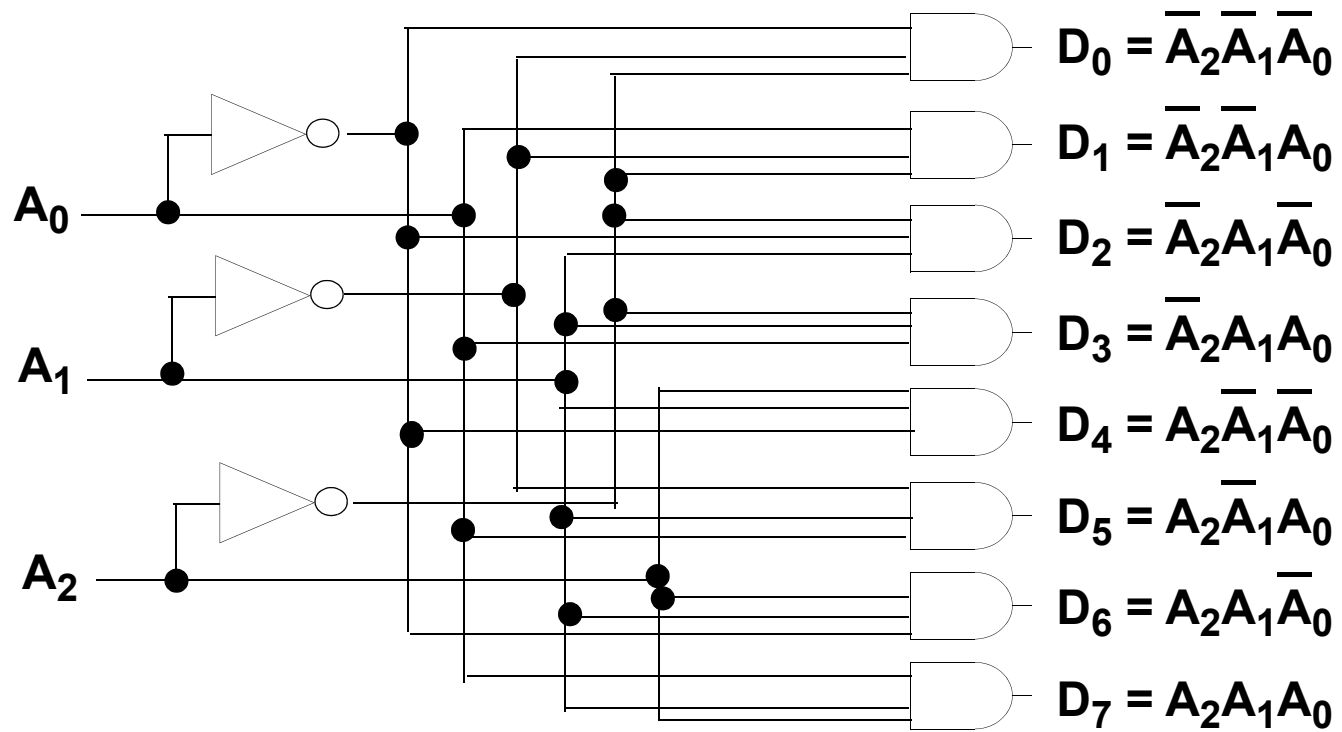
$$D_5 = A_2 \bar{A}_1 A_0$$

$$D_6 = A_2 A_1 \bar{A}_0$$

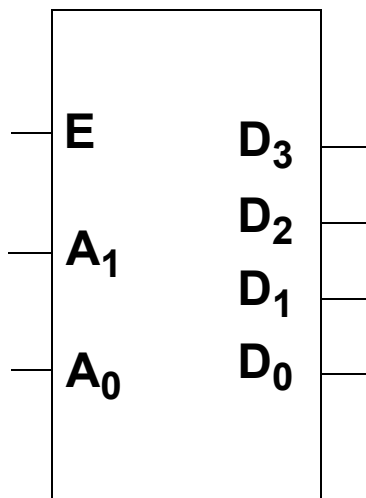
$$D_7 = A_2 A_1 A_0$$







2-to-4 Decoder with Enable Input



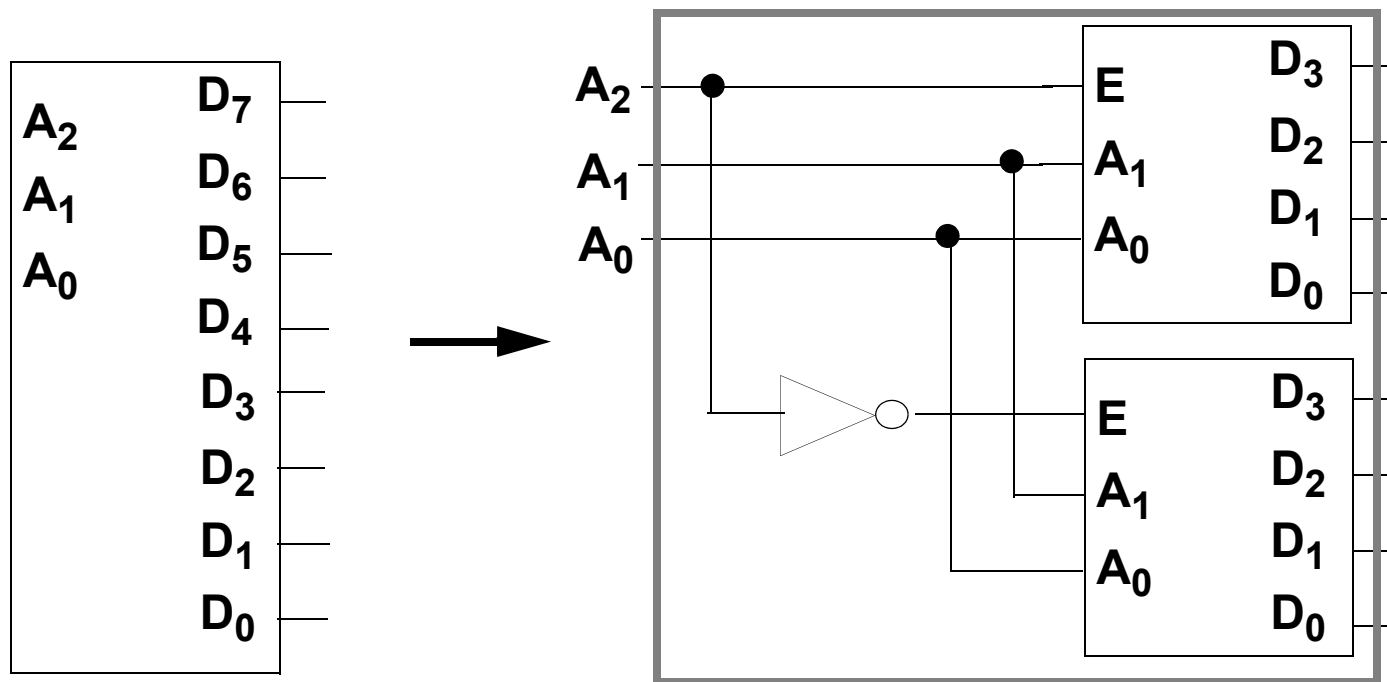
Inputs			Outputs			
E	A ₁	A ₀	D ₃	D ₂	D ₁	D ₀
1	0	0	0	0	0	1
1	0	1	0	0	1	0
1	1	0	0	1	0	0
1	1	1	1	0	0	0
0	-	-	0	0	0	0

2-to-4 Decoder with Enable Input

				Inputs				Outputs			
				E	A ₁	A ₀		D ₃	D ₂	D ₁	D ₀
—	E		D ₃	1	0	0		1	1	1	0
—	A ₁		D ₂	1	0	1		1	1	0	1
			D ₁	1	1	0		1	0	1	1
—	A ₀		D ₀	1	1	1		0	1	1	1
				0	-	-		1	1	1	1

Decoder Expansion

- When a certain size decoder is needed, if smaller sizes are available, then we need to expand the small size decoders.



Encoder

- An encoder : performs the inverse function of decoder, i.e. generate the binary code corresponding to the input value.

Example. 4-to-2 Encoder

Inputs				Outputs	
D_3	D_2	D_1	D_0	Y_1	Y_0
0	0	0	1	0	0
0	0	1	0	0	1
0	1	0	0	1	0
1	0	0	0	1	1

$Y_1 = ?$

$Y_0 = ?$

Improved Octal-to-Binary Encoder

- If more than one inputs are simultaneously 1, the output is not defined. --> Priority encoder removes this ambiguity.
 - When all inputs are 0, an output of all 0's are generated as if D_0 is 1.
- > Valid output set to on only when at least one input is 1.

Inputs				Outputs		
D_3	D_2	D_1	D_0	Y_1	Y_0	V
0	0	0	0	0	0	0
0	0	0	1	0	0	1
0	0	1	-	0	1	1
0	1	-	-	1	0	1
1	-	-	-	1	1	1

0	0	1	0
0	0	1	1
0	1	0	0
0	1	0	1
0	1	1	0
0	1	1	1
1	0	0	0
1	0	0	1
1	0	1	0
1	0	1	1
1	1	0	0
1	1	0	1
1	1	1	0
1	1	1	1

Inputs				Outputs		
D ₃	D ₂	D ₁	D ₀	Y ₁	Y ₀	V
0	0	0	0	0	0	0
0	0	0	1	0	0	1
0	0	1	-	0	1	1
0	1	-	-	1	0	1
1	-	-	-	1	1	1